

1 BASEBAND PREDISTORTION METHOD FOR MULTICARRIER TRANSMITTERS
23 FIELD OF THE INVENTION
4

5 This invention relates to transmitting and amplifying signals that at the baseband
6 are digital and more specifically to applying a predistortion algorithm to compensate for
7 inaccuracies introduced by amplifiers, filters and modulator in a multicarrier transmitter.
8 The biggest sources of imbalance tends to be baseband filters and the modulator. The
9 biggest source of gain inaccuracy tends to be the power amplifier.

10 BACKGROUND OF THE INVENTION

11 Wireless LAN standards require extremely good modulation accuracy and
12 accuracy of transmitted power. Amplitude and phase imbalances between the in-phase
13 and quadrature branches of the transmitter produce errors in the modulated signal.
14 Good balance is difficult to obtain due to component variations and due to the fact that
15 the amplitude and phase of the phase splitting circuits is frequency dependent. In
16 addition imbalances occur because of fluctuating temperatures.

17 SUMMARY OF THE INVENTION

18 According to an embodiment of the invention, four data symbols are used as raw
19 data, together with at least four transmitted symbols to arrive at several imbalance
20 parameters, which may be used to modify subsequent data symbols. The four
21 transmitted symbols may be sampled, and serve as the basis for calculating the energy
22 of the four transmitted symbols. A calculation of alpha, epsilon and gain imbalance
23 parameters may be made based on the four data symbols and the energy of the four
24 transmitted symbols. Alpha, epsilon and gain are stored. First quadrature
25 compensating of a next data symbol is done based on the alpha, epsilon, and gain to
26 produce a first quadrature compensated data symbol (FQCDS). Second quadrature
27 compensating the next data symbol is done based on the alpha, epsilon and gain to
28 produce a second quadrature compensated data symbol (SQCDS). First in-phase
29 compensating of the next data symbol is done to produce a first in-phase compensated
30 data symbol (FICDS). Second in-phase compensating of the next data symbol is done
31 to produce a second in-phase compensated data symbol (SICDS).

32 According to another embodiment of the invention, alpha, epsilon and gain are
33 available preset into appropriate storage. Each data symbol may be compensated based
34 on this preset information. First quadrature compensating of a data symbol is done

35 based on the alpha, epsilon, and gain to produce a first quadrature compensated data
36 symbol. Second quadrature compensating the data symbol is done based on the alpha,
37 epsilon and gain to produce a second quadrature compensated data symbol. First in-
38 phase compensating of the data symbol is done to produce a first in-phase
39 compensated data symbol. Second in-phase compensating of the data symbol is done
40 to produce a second in-phase compensated data symbol.

41 Among the benefits of the embodiments of the invention, the effects, at least of
42 one time, of the phase and amplitude imbalance may be stored. In addition gain
43 inaccuracies and local oscillator (LO) leakage may be measured and stored in a new
44 form as a set of imbalance parameters.

45 The first embodiment may routinely sample a transmitter output to obtain timely
46 imbalance parameters (referred to sometimes as α , ϵ and g) which may be influenced in
47 part, by data sampled at a baseband level, prior to operation of a inverse fast fourier
48 transform (IFFT). The routine updating of imbalance parameters may reflect a changing
49 environment, including variation of amplification on several frequencies and the effects
50 of changing temperatures.

51 The embodiments, once having obtained imbalance parameters, may apply
52 those imbalance parameters to predistort or compensate one or more baseband
53 symbols so that the amplified signal output of the amplifier has a narrower range of
54 errors in relation to phase, amplitude and gain.

55

56 BRIEF DESCRIPTION OF THE DRAWINGS

57 The disclosed inventions will be described with reference to the accompanying
58 drawings, which show important sample embodiments of the invention, wherein:

59 Fig. 1 shows a prior art Orthogonal Frequency Division Multiplexing (OFDM)
60 transmitter;

61 Fig. 2 shows a transmitter according to an embodiment of the invention; and

62 Fig. 3 shows a transmitter according to a factory-calibrated embodiment of the
63 invention.

64 DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENTS

65 Fig. 1 shows an Orthogonal Frequency Division Multiplexing (OFDM) transmitter
66 101, which is known in the art. Binary data enters the mapping block 103, which
67 converts the data into N pairs of I and Q signals, wherein N represents the number of
68 subcarrier frequencies that are modulated by the signals. These N pairs are fed into

69 Inverse Fast Fourier Transform (IFFT) 106. IFFT 106 produces the $S_I(t)$ (or in-phase)
 70 signal 107 and the $S_Q(t)$ (or quadrature) signal 109 according to the following formula:
 71

72
$$S_I(t) = \sum_{n=1}^{N/2} a_{N/2-n} \cos(n\omega_c t - \varphi_{N/2-n}) + a_{N/2+n+1} \cos(n\omega_c t + \varphi_{N/2+n+1}) \quad [1]$$

73
$$S_Q(t) = \sum_{n=1}^{N/2} -a_{N/2-n} \sin(n\omega_c t - \varphi_{N/2-n}) + a_{N/2+n+1} \sin(n\omega_c t + \varphi_{N/2+n+1}) \quad [2]$$

74 where a , φ , ω and N are the amplitude, phase and the frequency of the carriers,
 75 and N is the number of subcarriers, respectively. Digital to analog converter (DAC) 111
 76 converts $S_I(t)$ 107 to analog. Similarly DAC 113 converts $S_Q(t)$ 109 to analog. The
 77 analog signals enter the modulator 150 and are subsequently amplified by amplifier 151.
 78 The modulator may be a direct conversion-type of modulator.

79 Fig. 2 shows a transmitter according to an embodiment of the invention.
 80 Directional coupler 201 may obtain the waveform as amplified by amplifier, that is a
 81 transmitted symbol. Subsequently transmitted symbols are next symbols. The signal is
 82 provided to a squarer or power detector 203, which may be an analog device. An
 83 analog to digital converter follows 205. The signal may be integrated over the symbol
 84 duration using integrator 207, to provide an energy value 209 or energy of the
 85 transmitted symbol according to the following equation:

86
$$P_k = \int_0^{T_s} s_{o,k}^2(t) dt, \quad [3]$$

87 The term k represents the symbol number and T_s is the duration of one symbol.
 88 The energy 209 of four transmitted symbols thus is P_1 , P_2 , P_3 , and P_4 .

89
 90 Amplitude $a_{k,n}$ and phase $\Phi_{k,n}$ of subcarrier number n may be calculated as
 91 follows by S-calc 245:

92
$$a_{k,n} = \sqrt{d_{I,k,n}^2 + d_{Q,k,n}^2} \quad [4]$$

$$\phi_{k,n} = \arctan\left(\frac{d_{Q,k,n}}{d_{I,k,n}}\right)$$

93 where $a_{k,n}$ and phase $\Phi_{k,n}$ are the amplitude of subcarrier n and symbol k ,
 94 respectively. $d_{I,k,n}$ and $d_{Q,k,n}$ are the subcarrier in-phase and quadrature signals
 95 respectively for subcarrier n and symbol k .

96 S-calc 245 may calculate S parameters for the four symbols over the set of
 97 subcarriers as follows:

98
$$S_{1,k} = \sum_{n=1}^N (d_{I,k,n}^2 + d_{Q,k,n}^2) - 2 \sum_{n=1}^{N/2} (d_{I,k,N+1-n} d_{I,k,n} - d_{Q,k,N+1-n} d_{Q,k,n})$$
 [5]

99

100
$$S_{2,k} = \sum_{n=1}^{N/2} (d_{I,k,N+1-n} d_{Q,k,n} + d_{Q,k,N+1-n} d_{I,k,n})$$
 [6]

101

102
$$S_{3,k} = \sum_{n=1}^N (d_{I,k,n}^2 + d_{Q,k,n}^2) + 2 \sum_{n=1}^{N/2} (d_{I,k,N+1-n} d_{I,k,n} - d_{Q,k,N+1-n} d_{Q,k,n})$$
 [7]

103

104 where in-phase data $d_{I,1}..d_{I,N}$ and quadrature data $d_{Q,1}..d_{Q,N}$ 253 are available
105 from mapper 241.

106 One or several sets of four data symbols may be used during the sampling
107 period when imbalance parameters, gain and LO signal leakage are determined.

108 The S parameters form the basis for F parameters and H parameters as shown
109 below:

110
$$F_1 = S_{1,2}(S_{2,3}S_{3,4} - S_{2,4}S_{3,3}) + S_{1,3}(S_{2,4}S_{3,2} - S_{2,2}S_{3,4}) + S_{1,4}(S_{2,2}S_{3,3} - S_{2,3}S_{3,2})$$

111
$$F_2 = S_{1,1}(S_{2,4}S_{3,3} - S_{2,3}S_{3,4}) + S_{1,3}(S_{2,1}S_{3,4} - S_{2,4}S_{3,1}) + S_{1,4}(S_{2,3}S_{3,1} - S_{2,1}S_{3,3})$$

112
$$F_3 = S_{1,1}(S_{2,2}S_{3,4} - S_{2,4}S_{3,2}) + S_{1,2}(S_{2,4}S_{3,1} - S_{2,1}S_{3,4}) + S_{1,4}(S_{2,1}S_{3,2} - S_{2,2}S_{3,1})$$

113
$$F_4 = S_{1,1}(S_{2,3}S_{3,3} - S_{2,2}S_{3,3}) + S_{1,2}(S_{2,1}S_{3,3} - S_{2,3}S_{3,1}) + S_{1,3}(S_{2,2}S_{3,1} - S_{2,1}S_{3,2})$$

114
$$H_1 = S_{2,2}(S_{1,4} - S_{1,3}) + S_{2,3}(S_{1,2} - S_{1,4}) + S_{2,4}(S_{1,3} - S_{1,2})$$

115
$$H_2 = S_{2,1}(S_{1,3} - S_{1,4}) + S_{2,3}(S_{1,1} - S_{1,4}) + S_{2,4}(S_{1,1} - S_{1,3})$$

116
$$H_3 = S_{2,1}(S_{1,4} - S_{1,2}) + S_{2,2}(S_{1,1} - S_{1,4}) + S_{2,4}(S_{1,2} - S_{1,1})$$

117
$$H_4 = S_{2,1}(S_{1,2} - S_{1,3}) + S_{2,2}(S_{1,3} - S_{1,1}) + S_{2,3}(S_{1,1} - S_{1,2}).$$
 [8]

118

119 The energy 209 of the four transmitted symbols may contribute to the calculation
120 of the P_{LO} local oscillator signal power as follows:

121

122
$$P_{LO} = -\frac{P_1 F_1 + P_2 F_2 + P_3 F_3 + P_4 F_4}{P_1 H_1 + P_2 H_2 + P_3 H_3 + P_4 H_4},$$
 [9]

131 The S parameters from S-calc 245 and the P parameters from 209 may be used
 132 to compute the epsilon, alpha and g and store the values as imbalance parameters to a
 133 cache or storage 250:

134

$$135 \quad \epsilon = \sqrt{\frac{P_1(S_{2,3}(P_{LO} + S_{3,2}) - S_{2,1}(P_{LO} + S_{3,3})) + P_2(S_{2,1}(P_{LO} + S_{3,3}) - S_{2,3}(P_{LO} + S_{3,1})) + P_3(S_{2,2}(P_{LO} + S_{3,1}) - S_{2,1}(P_{LO} + S_{3,2}))}{P_1(S_{1,3}S_{2,2} - S_{1,2}S_{2,3}) + P_2(S_{1,1}S_{2,3} - S_{1,3}S_{2,1}) + P_3(S_{1,2}S_{2,1} - S_{1,1}S_{2,2})}}$$

136

$$137 \quad \alpha = \arcsin\left(\frac{-1 \frac{P_1(S_{1,2}(P_{LO} + S_{3,3}) - S_{1,3}(P_{LO} + S_{3,2})) + P_2(-S_{1,1}(P_{LO} + S_{3,3}) + S_{1,3}(P_{LO} + S_{3,1})) + P_3(S_{1,1}(P_{LO} + S_{3,2}) + S_{1,2}(-S_{3,1} - P_{LO}))}{4\epsilon}}{P_1(S_{1,2}S_{2,3} - S_{1,3}S_{2,2}) + P_2(S_{1,3}S_{2,1} - S_{1,1}S_{2,3}) + P_3(S_{1,1}S_{2,2} - S_{1,2}S_{2,1})}\right)$$

138

139 [11]

$$140 \quad g_t = \frac{4P_1}{\epsilon S_{1,1} + 4\epsilon \sin(\alpha) S_{2,1} + S_{3,1} + P_{LO}} \quad [12]$$

141 The epsilon, alpha and g values may then be stored unchanged in 250.

142 Alternatively, the epsilon, alpha and g values may be updated whenever an additional
 143 data symbol in the form of in-phase data and quadrature data 253 is available, or less
 144 frequently.

145 Yet another arrangement for determining epsilon, alpha and g values includes
 146 calculating a first alpha, first epsilon and a first gain based on the energy of the at least
 147 four transmitted symbols; and calculating a second alpha, second epsilon and a second
 148 gain based on the energy of the next data symbol. The final steps to reach the alpha,
 149 epsilon and gain values may include calculating a alpha based on a average of the first
 150 alpha and the second alpha; calculating a epsilon based on a average of the first epsilon
 151 and the second epsilon; and calculating a gain based on a average of the first gain and
 152 the second gain. Thus during a compensation period, the imbalance parameters in use
 153 may be averaged values. Many forms of averaging may be used, including weighting a
 154 more recent value more heavily, e.g. weighting a second alpha heavier than a first alpha.

155 The duration when the compensator provides the compensated data signals is
 156 known as the compensation period. The compensator 251 may operate in a sampling
 157 period acquisition mode where no changes are made to data symbols provided to the
 158 compensator, and such symbols are placed onto the IFFT-bus 261 unchanged by the
 159 compensator. The compensator may operate in a feedback mode during a
 160 compensation period where the compensator 251 provides the compensated in-phase
 161 baseband, i.e. first in-phase compensated data symbol (FICDS) 263, and a second in-

162 phase compensated data symbol (SICDS) 265, and compensated quadrature baseband,
 163 i.e. a first quadrature compensated data symbol (FQCDS) 262, second quadrature
 164 compensated data symbol (SQCDS) 264, signals to the IFFT 271.

165 Fig. 3 shows an embodiment that dispenses with the use of a persistent
 166 feedback loop in favor of testing the transmitter output, data symbols at the time of
 167 manufacture, and storing the resultant imbalance parameters, epsilon, alpha and gain, in
 168 a storage 350 which may be non-volatile. The factory calibration apparatus may sample
 169 symbols, denoted by $d_{I,1}..d_{I,N}$ and $d_{Q,1}..d_{Q,N}$ 353 as well as sample and amplifier output
 170 301 to derive, by methods similar to those used in Fig. 2, to obtain the epsilon, alpha and
 171 gain applicable to symbols transmitted by the amplifier. The data symbols 353 may
 172 each comprise a first quadrature subcarrier 354, a first in-phase subcarrier 355, a
 173 second quadrature subcarrier 356 and a second in-phase subcarrier 357. Thus, a
 174 feedback loop may not be required in the final product that is shipped.

175 The hardware for the factory-calibrated embodiment may include a compensator
 176 351 reading from the storage 350. Such an apparatus may be inserted to intercept the
 177 signals of the prior-art mapper 341, changing the in-phase baseband and quadrature
 178 baseband 353 signals to compensated data symbols 361. IFFT 371 produces the I
 179 signal 307 and the Q signal 309 by means known in the art. Modulator 381 may operate
 180 as an OFDM and may be followed by amplifier 391.

181 Once the alpha, epsilon and gain values are known, by the feedback loop in fig.2,
 182 compensation of the current data symbol presented to the compensator 251 may be
 183 performed in an operation known as compensating. Each subcarrier component of the
 184 current data symbol may be referred to as a next symbol in relation to a data symbol that
 185 provided data for computing the alpha, epsilon and gain values of the storage 250.
 186 Compensator 251 may perform at least four operations. Compensator 251 may perform
 187 at least one first quadrature compensating of a next data symbol, thus obtaining the
 188 FQCDS, or $d'_{Q,n}$:

$$189 d'_{Q,n} = \frac{g_w}{g} \frac{d_{Q,n}(1 + \varepsilon \cos(\alpha)) + d_{Q,(n+N/2)}(1 - \varepsilon \cos(\alpha)) + \varepsilon \sin(\alpha)(d_{I,n} - d_{I,(n+N/2)})}{2\varepsilon \cos(\alpha)}, [13]$$

190 for each n valued at 1 through $N/2$. Compensator 251 may perform at least one second
 191 quadrature compensating of a next data symbol, thus obtaining the SQCDS or $d'_{Q,n}$:

$$193 d'_{Q,n} = \frac{g_w}{g} \frac{d_{Q,(n-N/2)}(1 - \varepsilon \cos(\alpha)) + d_{Q,n}(1 + \varepsilon \cos(\alpha)) + \varepsilon \sin(\alpha)(d_{I,n} - d_{I,(n-N/2)})}{2\varepsilon \cos(\alpha)}, [14]$$

195 for each n valued at N/2+1 through N. Compensator 251 may perform at least one first
196 in-phase compensating of a next data symbol, thus obtaining the FICDS, or $d'_{I,n}$:

$$197 d'_{I,n} = \frac{g_w}{g} \frac{d_{I,n}(1 + \varepsilon \cos(\alpha)) + d_{I,(n+N/2)}(\varepsilon \cos(\alpha) - 1) - \varepsilon \sin(\alpha)(d_{Q,n} + d_{Q,(n+N/2)})}{2\varepsilon \cos(\alpha)}, [15]$$

198
199 for each n valued at 1 through N/2. Compensator 251 may perform at least one second
200 in-phase compensating of a next data symbol, thus obtaining the SICDS, or $d'_{I,n}$:

$$201 d'_{I,n} = \frac{g_w}{g} \frac{d_{I,(n-N/2)}(\varepsilon \cos(\alpha) - 1) + d_{I,n}(1 + \varepsilon \cos(\alpha)) - \varepsilon \sin(\alpha)(d_{Q,n} + d_{Q,(n-N/2)})}{2\varepsilon \cos(\alpha)}, [16]$$

202

203 for each n valued at N/2+1 through N.

204 In each of the foregoing four equations, g_w is the wanted gain, which may be set
205 to a value desired by the operator of the transmitter. If it is desired to use an averaged
206 value of α , ε and g , those values may be used if previously stored in cache 250.

207 Although the invention has been described in the context of particular
208 embodiments, various alternative embodiments are possible. For example, other
209 transmitters that have baseband I and Q signals of the form shown in equations [1] and
210 [2] may benefit from compensation as shown herein. In addition, calculation of
211 imbalance parameters may occur following the transmission of most symbols, or less
212 frequently, e.g. near the beginning of a packet. Thus, while the invention has been
213 particularly shown and described with respect to specific embodiments thereof, it will be
214 understood by those skilled in the art that changes in form and configuration may be
215 made therein without departing from the scope and spirit of the invention.

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